# Assessment of long-term extreme response of a floating support structure using the environmental contour method

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ABSTRACT: This paper analyses the extreme response of a semi-submersible floating support structure for a wind turbine installed in the northern North Sea. The environmental contour method is used to directly estimate the extreme sea states that are used thereafter to calculate the long-term extreme response of the semi-submersible. This study focuses on the 1D and 2D environmental contours model based on the inverse first-order reliability method (IFORM). The significant wave height and peak period are the two environmental random variables used to estimate the contour. The response amplitude operator of the heave, surge, and pitch in head waves are estimated using the 3D panel method. A full long-term analysis is performed and compared with that estimated by adopting the 1D and 2D model. The results show a remarkable deviation between the full long-term analysis and the long-term obtained by the environmental contour method except in the heave response.

# 1 INTRODUCTION

Estimating the long-term extreme responses is of crucial importance in the reliability-based design of any floating offshore wind turbine. Among others, two uncertainties are associated with such a structural reliability problem: (1) the environmental load, and the (2) extreme response. In an attempt to decouple these uncertainties, Winterstein et al. (1993) presented a method to construct environmental contours based on the inverse first-order reliability method (FORM). Nowadays, the FORM is widely used to solve and analyses reliability problems for ships and offshore structures, e.g. Teixeira & Guedes Soares (2005), Teixeira & Guedes Soares (2009) and Guedes Soares et al. (2010).

The general idea of constructing environmental contour is based on identifying the extreme sea states corresponding to a certain probability of failure  $(P_t)$  and using these values to calculate the long-term extreme response. Winterstein & Engebretsen (1998) applied this concept and described procedures to estimate the extreme design loads and response for both spar buoy and a tension leg platform (TLP). However, it has been noted that neglecting the response variability in these procedures underestimates the extreme response, e.g. in case of the TLP, the median of the 100-year return period response was under estimated by 1.3 to 1.4 times compared to the actual response, whereas these values were much more in the spar buoy case. Since this method was accurate enough, many researchers adopted it in wind turbine applications.

Karmakar et al. (2016) used the aforementioned environmental contour approach to investigate the long-term extreme bending moments acting on the turbine's blade root and on the tower base for a spar and a semi-submersible type of floaters. They took into consideration the wind speed, the significant wave height and the peak period. Agarwal & Manuel (2009) determined the long-term extreme load acting on the offshore wind turbine foundation using an efficient inverse reliability approach. Furthermore, Karimirad & Moan (2011) focused on the extreme coupled wind and wave induced motion for a floating offshore wind turbine of a spar type.

However, the results of the conventional environmental contour method for some responses of wind turbines have been also found to be largely under-predicted as shown by Saranyasoontorn & Manuel (2004), Agarwal & Manuel (2009) and Li et al. (2016). Li et al. (2017) overcame this problem by presenting a modified environmental contour method (MECM), which is also based on the FORM considering the active survival strategy to be better suited for offshore wind turbines. The environmental contour can be 1D, 2D or 3D depending on the number of environmental random variables taken into consideration.

In this study only the 1D and 2D contour are considered. In order to construct the contours of the environmental parameters, it is necessary to identify the joint distribution of the environmental parameters. Many studies have been done on the joint distribution of significant wave height  $(H_s)$ and wave period  $(T_p)$  in the northern North Sea, which results in a marginal Weibull distribution for  $H_s$  and a log-normal conditional distribution for  $T_p$ , e.g. Haver (1985), Ferreira & Guedes Soares (2002), DNV (2010), Vanem & Bitner-Gregersen (2015) and Lucas & Guedes Soares (2015).

Alternatively, a full long-term analysis could be done instead of the environmental contour method. The full long-term analysis combines the response distributions of all short-term environmental conditions according to their probability of occurrence. Guedes Soares (1993) and Guedes Soares & Schellin (1996) proposed a methodology for the long-term formulation of non-linear wave induced vertical bending moment. Furthermore, Chakrabarti (2005) and Nejad et al. (2013) described three different approaches to estimate characteristic long-term extreme values based on all peak values, all short term extreme values and the up-crossing rate.

The disadvantage of this method is the large number of simulations required, which is considered by Videiro & Moan (1999) not efficient. Furthermore, Raed et al. (2016) adopted the full long-term analysis to estimate the long-term Morison's wave load acting on the OC4 floating structure. In order to reach the final stage for these calculations, it was necessary to estimate the Response Amplitude Operators (RAO) of the floating structure. To do that, the linear frequencydomain analysis was adopted in this study and a detailed explanation for this type of analysis is described by Newman (1977), Faltinsen (1990).

This paper presents the long-term extreme response acting on the OC4 wind turbine floating support structure (semi-submersible) located in the northern North Sea. The one-dimensional and the two-dimensional environmental contour models based on the inverse FORM are adopted to estimate the long-term extreme response for the semi-submersible. The significant wave height and the peak period are the environmental variables considered in this study. The Weibull distribution is adopted for  $H_s$  and a log-normal distribution for  $T_p$  as done by Haver (1985). ANSYS AQWA is used to predict the heave, surge, and pitch RAOs. Thereafter, the responses are estimated by multiplying the JONSWAP spectrum for each sea state  $(H_{a}, T_{b})$  by the square of the RAO. The long-term extreme response resulting from the 1D and 2D environmental model are compared with the fully long-term analysis based the scatter diagram in the northern North Sea, (Moan et al. 2005).

## 2 RELIABILITY BASED ANALYSIS

The limit sate function for any reliability problem can be defined as follows:

$$g(x) = y_{capacity} - Y(x) \tag{1}$$

where g(x) is the limit sate function;  $y_{capacity}$  is the strength; and the Y(x) is the load acting on the structure. The reliability (*R*) is related to the probability of failure (*P*<sub>d</sub>) and the relation is given by:

$$R = 1 - P_f = P[g(x) > 0] = \int_{g(x) > 0} f_x(x) dx$$
(2)

Since this integration is often difficult to solve due to the complicated joint distribution of the random variables. The first-order reliability method (FORM) and second-order reliability method are used (SORM), (see Melchers 1999 for more details). The relation between the reliability index ( $\beta$ ) and the probability of failure ( $P_i$ ) is given by:

$$\beta = \Phi^{-1}(1 - P_f) \tag{3}$$

where  $\Phi$  is the standard Gaussian probability distribution.

## 2.1 Environmental contour

The environmental contour method is an effective, risk-based, time saving approach. The widely used environmental contour method is based on the Rosenblatt transformation. This is done by transforming the vector of environmental variables, **X**, into a vector **U** of independent normally distributed variable, (Vanem 2017). Figure 1 illustrates the concept of transformation. This method is based on the inverse FORM since the  $P_f$  is assumed despite of computed.

The probability of failure  $(P_i)$  is given by:

$$P_f = \frac{T_{ss}}{365 \ 24 \ T_r}$$
(4)

where  $T_{ss}$  is the sea state duration in hours;  $T_r$  is the return period in years; and the ( $360 \times 24$ ) factor is to convert the number of years to hours. If the joint density function of all variables is known the transformation of original design variables (dependent and non-normal) to independent standard normal variables can be performed using the Rosenblatt transformation as will be described below.



Figure 1. Illustration of the transformation from the normal space to the physical space, Huseby et al. (2013).

#### 2.1.1 One-dimensional (1D) model

In case of the 1D model the reliability index ( $\beta$ ) is assumed to be equal to random variable ( $u_i$ ) in the normal space, as shown in

Figure 2 and the other environmental random variables are assumed to be zero.

According to the 1-D model, the probability of exceedance is related to the standard normal space by:

$$u_1 = \beta; \ u_2 = 0; \ u_3 = 0$$
 (5)

where  $\beta$  is the reliability index related to the failure probability ( $P_j$ ) by eq.(3). Thereafter, using the Rosenblatt transformation scheme, the physical plan's points are obtained by:

$$\Phi(u_1) = F_X(X_1) 
\Phi(0) = F_{X_2|X_1}(X_2|X_1)$$
(6)

## 2.1.2 Two-dimensional model

In the two-dimensional environmental contour model, the random variables in the normal space are assumed to be in a circle with radius equal to  $\beta$ , as shown in Figure 3.

where  $u_1$  and  $u_2$  are given by:

$$u_1 = \beta \cos\theta; \ u_2 = \beta \sin\theta; \ u_3 = 0 \tag{7}$$



Figure 2. One dimensional model illustration; (Karmakar et al. 2016).



Figure 3. Geometric representation of the 2D model representation in the U-space, (Karmakar et al. 2016).

where  $\theta$  is the angle between  $\beta$  and  $u_i$ , and vary between  $0^\circ < \theta < 360^\circ$ .

Similarly, by applying the Rosenblatt transformation, the physical plan points are obtained by:

$$\Phi(u_1) = F_X(X_1) \Phi(u_2|u_1) = F_{X_2|X_1}(X_2|X_1)$$
(8)

Hence, for a given marginal distribution for  $X_1$  and conditional distribution for  $X_2$ , the Rosenblatt transformation results in:

$$X_{1} = F_{X}^{-1}(\Phi(u_{1}));$$
  

$$X_{2} | X_{1} = F_{X_{2}|X_{1}}^{-1}(\Phi(u_{2}|u_{1}))$$
(9)

where the joint distribution of the two environmental parameters  $(X_i, X_2)$  are given in the next section.

#### 2.2 Joint probability distribution of $H_s$ and $T_p$

The marginal distribution of the significant wave height  $F_{Hs}(h)$  is given by the Weibull distribution as follows: (Winterstein et al. 1993)

$$F_{H_s}(h) = 1 - \exp\left(-\left(\frac{h}{2.822}\right)^{1.547}\right)$$
(10)

whereas the conditional distribution of the peak period  $F_{T_{P|Hs}}(T_{P}|H_{s})$  is given by a log-normal distribution, which has mean and variance as follows: (Winterstein et al. 1993)

$$\mu = E(T_p | H_s) = 1.59 + 0.42 \ln(H_s + 2)$$
(11)

$$Var = 0.005 + 0.085 \exp(-0.13H_s^{1.34})$$
(12)

#### **3 RESPONSE IN IRREGULAR WAVES**

The general equation of motion for the system is:

$$(\mathbf{M} + \mathbf{A})\zeta + \mathbf{B}\zeta + \mathbf{C}\zeta = \mathbf{F}(t)$$
(13)

Table 1. Fitted parameters for the 2 parameters Weibull distribution for  $H_s$  and conditional log-normal distribution for  $T_p$  according to Eqs. (10), (11) and (12); Northern North Sea.

Weibull $(H_s)$		Shape 1.547	Scale 2.822		
		a1	a2	a3	
$\begin{array}{c} \text{Lognormal} \\ (T_p) \end{array}$	μ	1.59	0.42	2	
	$\sigma^2$	<i>b1</i>	<i>b2</i>	<i>b3</i>	<i>b4</i>
		0.005	0.085	-0.13	1.34

where **M** is the mass of the structure; **A** is the added mass matrix; **B** and **C** are the damping coefficient and the restoring coefficient respectively; **F** is the hydrodynamic excitation;  $\zeta$  is the semi-submersible displacement from its mean position. The response of a linear motion is obtained by multiplying the wave energy spectrum  $S_w(\omega)$  by the square of RAO for the appropriate motion as follows:

$$S_{R}(\omega) = S_{w}(\omega)RAO_{j}^{2}(\omega)$$
(14)

$$RAO(\omega) = \left(\frac{x_j}{\zeta_{wave}}\right) \tag{15}$$

where  $x_j$  is the motion displacement and  $\zeta_{wave}$  is the wave amplitude in [m]

#### 3.1 JONSWAP Spectrum

The Joint North Sea Wave Project (JONSWAP) spectrum is used in this study to estimate the energy of the sea state in the northern North Sea. The JONSWAP spectrum is given by: (Journée & Massie 2001)

$$S(\omega) = \frac{320H_s^2}{T_p^4} \omega^{-5} \exp\left(\frac{-1950}{T_p^4} \omega^{-4}\right) \gamma^4$$
(16)

where

$$A = \exp\left\{-\left(\frac{\frac{\omega}{\omega_{p}}-1}{\sigma\sqrt{2}}\right)^{2}\right\}$$
(17)

where  $\omega$  is the wave frequency in rad/sec;  $\gamma$  is the peakedness factor and is equal to 3.3;  $\omega_p$  is the peak period in rad/sec and is given by:

$$\begin{split} \omega_{p} &= \frac{2\pi}{T_{p}} \\ \sigma &= 0.07 \quad \text{if } \omega < \omega_{p} \\ \sigma &= 0.09 \quad \text{if } \omega > \omega_{p} \end{split}$$

## 4 FULL LONG-TERM ANALYSIS

The idea behind the long-term extreme load analysis is to obtain an estimation of the extreme load with a given probability of exceedance by accounting the load from various short-term wave conditions, as presented by Guedes Soares (1998). The probability of exceeding a given level x of wave amplitude is given by the Rayleigh distribution as:

$$Q_s(X|R) = \exp\left(\frac{-x^2}{2R}\right),\tag{18}$$

where *R* is the variance of the process. The Gaussian process assumes that in the frequency domain the process is completely described by its power spectrum. So, the area under the spectrum is directly related to the variance. The variance (*R*) for each combination of parameters is given by:

$$R = m_0 = \int_0^\infty S_R(\omega, H_s, T_p, D, h, Z, H)$$
(19)

where  $S_R$  is the response spectrum which is given by eq. (14),  $\omega$  is the wave frequency,  $H_s$  is the significant wave height,  $T_p$  is the peak period, D is the member diameter, h is the water depth, Z is the draft and H is the wave height. The basic formulation applicable to calculate the long-term distribution of wave amplitude is given by:

$$Q_L = \int_0^\infty Q_S(x|r) \cdot f_R(r) dr$$
(20)

where  $Q_s$  is the short-term distribution given by eq.(18) and  $f_R$  is the probability density function of the sea state variance and is obtained from the scatter diagram. The number of years corresponds to the full long-term distribution is given also by eq. (4).

## 5 RESULTS AND DISCUSSION

The model of the semi-submersible used in this study is shown in Figure 4, which consists of three side columns and one main column that support the wind turbine. Table 2 shows the main characteristics of the floating structure as prescribed by Robertson et al. (2014).

The analysis was made using ANSYS AQWA to estimate the heave, surge and pitch RAOs in head waves. The environmental variables under consideration are the significant wave height  $(H_y)$  and the peak



Figure 4. Semi-submersible geometry.

Main Column diameter	6.5 m
Offset column diameter	12 m
Bottom column diameter	24 m
Bracing diameter	1.6 m
Draft	20 m
Mass including ballast	1.3473E+7 kg
Center of mass below SWL	13.46 m
Roll moment of inertia $I_{xx}$ about COG	6.827E+9 kg.m <sup>2</sup>
Pitch moment of inertia $(I_{yy})$ about COG	6.827E+9 kg.m <sup>2</sup>
Yaw moment of inertia $(I_{ZZ})$ about COG	1.226E+10 kg.m <sup>2</sup>

Table 2. Main characteristics of the OC4 semisubmersible.

period  $(T_p)$ . Regarding the 1D model,  $H_s$  is considered as random and  $T_p$  is estimated directly from the log-normal distribution by substituting the  $H_s$  value corresponding to each  $P_f$ . The probability of failure is calculated using eq.(4) for each return period  $(T_f)$  and for  $T_{ss}$  equal to 3 hours. Thereafter, the reliability index ( $\beta$ ) estimated for 10 years return period is 3.98, 4.19 for 25-years return period, whereas for 50 and 100 years are 4.35 and 4.5, respectively, as shown in Table 3. Winterstein et al. (1993) presented the Weibull distribution parameters and the lognormal distribution parameters for  $H_s$  and  $T_p$ , respectively as shown in the aforementioned Table 1.

Adopting the 1D environmental contour model results in increasing Hs as the return period increases as shown in the left-hand plot of Figure 5. Comparing the results obtained for the 25, 50 and 100 years, it is observed that increasing the return period by 50% results in increasing the values of Hs by 3.7% and the Tp by 1.2% on average, as shown in the right-hand plot of Figure 5. It can be noted that, the behaviour of the Hs and Tp is nearly linear since Tp increases with increasing Hs.

The 2D environmental contour model differs from the 1D model in the number of the variable's points  $(H_s, T_p)$  constructing the contour. The 1D model results in only one point for each return period, whereas, the 2D environmental contour results in a large number of points depend on the tangent lines around the circle of radius  $\beta$  in the normal space (Figure 1). Figure 6 shows the 2D environmental contour using the inverse first-order reliability method (IFORM) for 10, 25, 50 and 100 years return period based on 60 tangent lines. The number of tangent lines selected gives reasonable and visually smooth contours, as shown in Figure 6.

Table 4 shows the values of  $(H_{\gamma}, T_{p})$  along the contours for 10, 25, 50 and 100-years using the 2D model approach. Only the values up to 102 degrees are presented since higher angles result in lower values for  $H_{s}$  and  $T_{p}$ . These contour values will be used in the response analysis of heave, surge and pitch motions

Table 3. Values of the 1D environmental contour.

Return period [yrs.]	(Pf)	(β)	Hs [m]	Tp [s]
10	1.141E-05	3.98	12.73	15.18
25	4.566E-06	4.19	13.45	15.48
50	2.283E-06	4.35	13.98	15.70
100	1.142E-06	4.50	14.50	15.92
			-	



Figure 5. 1D environmental contour.



Figure 6. 2D contour using inverse FORM.

for the semi-submersible under consideration. The 100-years extreme condition estimated by Winterstein et al. (1993) was  $H_s = 14.5$  m and  $T_p = 15.9$  s, and it can be observed that this value agrees well with the values shown in Table 4. As expected, the maximum values of  $H_s$  and their corresponding  $T_p$ 's values obtained by the 2D model at 0° are identical to those obtained by the 1D model. Despite that, the extreme response will not be obtained at the maximum  $H_s$  values as will be shown later.

As shown in Table 4, increasing the return period by 50% (e.g. from 25 years to 50 years) results in increasing the  $H_s$  by 3.13% on average between the intervals [0°, 90°] and [270°, 360°], while decreasing the  $H_s$  by 20.41% on average in the interval [90°,270°]. Regarding the conditional  $T_p$ , increasing the return period in general tends to increase its values except in the interval [180°,300°]. Strictly, increasing the return period from 25 to 50 years lead to increase the  $T_p$  by 1.46% on average and decrease it by 2.9% on average in the interval [180°,300°].

Table 4. Points selected along the 2D environmental contour.

$(H_{s'} T_p)$					
$\theta^{o}$	10-years	25-years	50-years	100-years	
0 6 12 18 24 30 36 42 48 54 60	(12.73, 15.18) (12.66, 15.67) (12.44, 16.12) (12.08, 16.53) (11.59, 16.90) (10.97, 17.27) (10.25, 17.64) (9.44, 18.07) (8.55, 18.60) (7.61, 19.26) (6.64, 20.10)	(13.45, 15.48) (13.37, 16,00) (13.14, 16.46) (12.75, 16.88) (12.23, 17.26) (11.57, 17.62) (10.8, 17.99) (9.93, 18.41) (8.98, 18.94) (7.97, 19.63) (6.93, 20.54)	(13.98, 15.71) (13.90, 16.23) (13.65, 16.71) (13.25, 17.14) (12.70, 17.52) (12.01, 17.88) (11.20, 18.24) (10.28, 18.66) (9.29, 19.18) (8.23, 19.89) (7.15, 20.84)	(14.50, 15.92) (14.42, 16.46) (14.16, 16.9) (13.74, 17.39) (13.16, 17.78) (12.44, 18.14) (11.59, 18.49) (10.64, 18.89) (9.59, 19.42) (8.49, 20.14) (7.36, 21.13)	
66 72 78 84 90 96 102	$\begin{array}{l} (5.67, 21.09)\\ (5.67, 21.09)\\ (4.72, 22.18)\\ (3.81, 23.23)\\ (2.97, 24.05)\\ (2.23, 24.43)\\ (1.59, 24.23)\\ (1.09, 23.44) \end{array}$	$\begin{array}{c} (6.52, 26.54)\\ (5.89, 21.65)\\ (4.87, 22.92)\\ (3.90, 24.19)\\ (3.01, 25.23)\\ (2.23, 25.77)\\ (1.56, 25.63)\\ (1.04, 24.80) \end{array}$	(6.06, 22.05) (4.99, 23.45) (3.97, 24.90) (3.04, 26.11) (2.23, 26.79) (1.54, 26.70) (1.00, 25.84)	$\begin{array}{c} (1.52, 21.12)\\ (6.21, 22.42)\\ (5.10, 23.96)\\ (4.04, 25.58)\\ (3.08, 26.99)\\ (2.23, 27.82)\\ (1.52, 27.79)\\ (0.97, 26.90) \end{array}$	



Figure 7. (a) Heave RAO, (b) Surge RAO and (c) Pitch RAO.

The linear body response in the frequencydomain was estimated by calculating the motions Response Amplitude Operator (RAO) of the semisubmersible using ANSYS AQWA. The numerical model was analysed in a frequency range between 0.34 rad/s and 1.25 rad/s. Figure 7 shows the RAOs at zero-degree wave heading of the motions under consideration; plot (a), (b) and (c) present the heave, surge and pitch motion, respectively.

Regarding the heave RAO, as expected, at low frequencies the semi-submersible has an amplitude equal to the exciting waves. Moreover, the heave excitation is maximum at the heave natural frequency (0.36 rad/s) and reaches 7.2 m/m which compare well with some of the results published in Robertson et al. (2014). The surge and pitch RAOs are shown in Figure 7(b) and (c), respectively. It can be noted the pitch-surge coupling through the peak at the pitch natural frequency (0.32 rad/s). Furthermore, it is expected that the peak in the pitch-surge coupling in the no-wind case, which is the case under consideration, is higher than if we consider the wind turbine installed and in an operation condition.

Table 5 shows the response values of the three modes of motion under consideration (heave, surge and pitch) resulting from adopting the 1D environmental contour model. As expected, the 100-years return period, which is equivalent to  $\beta = 4.5$  always gives the highest response corresponds to the highest sea state. However, the 1D model results in only one extreme sea state that causes the extreme response for all motions under consideration at the same time, which is not realistic. It can be observed that increasing the heave, surge and pitch responses by 11%, 4% and 10.7% on average, respectively.

The 2D environmental contour results are presented in Table 6 and Table 7. It can be observed that the maximum response for each motion corresponds to a different sea state.

Table 5. Long-term extreme response results from the 1D model.

Return	1D model						
[yrs.]	$H_s[m]$	$T_p[s]$	Heave [m]	Surge [m]	Pitch [ <sup>0</sup> ]		
10 25 50	12.73 13.45 13.98	15.18 15.48 15.71	8.78 10.26 11.54	1.68 1.75 1.77	0.66 0.79 0.89		
100	14.50	15.92	12.95	1.90	0.99		

Table 6.Long-term extreme response results from the2D model (heave and pitch motions).

Return	Heave motion			Pitch motion		
[yrs.]	$H_{s}[m]$	$T_p[s]$	amp[m]	$H_s[m]$	$T_p[s]$	amp [º]
10	10.97	17.27	14.88	12.08	16.53	0.91
25 50	12.23 13.25	17.26 17.14	16.56 17.62	13.14 13.65	16.46 16.71	0.99 1.03
100	13.74	17.40	18.87	14.42	16.46	1.09

Table 7.Long-term extreme response results from the2D model (surge motion).

	Surge motion				
Return period [yrs.]	$H_{s}[m]$	$T_p[s]$	amp [m]		
10	12.08	16.53	1.75		
25	13.14	16.46	1.90		
50	13.65	16.71	1.97		
100	13.74	17.34	2.09		

In case of 50-years return period, the heave maximum response is equal to 14.9 m and is obtained in a sea state (11 m, 17 s), while the pitch maximum response is equal to 0.90 and occurring at a sea state (12.1 m, 16.5 s). Increasing the return period by 50% results in higher the extreme amplitude of heave, pitch and surge by 6.3%, 4.7% and 4.6% on average, respectively.

Figure 8, Figure 9 and Figure 10 illustrate a comparison between the extreme response for the semi-submersible obtained by the 1D model, the 2D model and the full long-term analysis in the northern North Sea for the heave, surge and pitch responses, respectively. Regarding the heave response shown in Figure 8, the full long-term analysis agrees well with the 2D model results until approximately 30-years return period. Thereafter, the results diverge until the end.

The full-long term analysis overestimates the heave response's value by around 10%, after 30-yr return period, compared to the 2D model, whereas the 1D model strongly under predicts the results. In Figure 9 and Figure 10, the results show that the



Figure 8. Comparison between the results obtained by both the 1D and 2D model with the full long-term analysis for heave response.



Figure 9. Comparison between the results obtained by both the 1D and 2D model with the full long-term analysis for surge response.



Figure 10. Comparison between the results obtained by both the 1D and 2D model with the full long-term analysis for pitch response.

full long-term analyses result in 65% and 72% higher response for the surge and pitch, respectively compared to the 2D model. On the other hand, the results obtained by adopting the 1D and 2D model agree well with each other's as shown in Figure 9 and Figure 10.

# 6 CONCLUSIONS

In the present study, the 1D and 2D environmental contour models based on the IFORM are used to estimate the extreme sea states in the northern North Sea. The long-term extreme responses, for the heave, surge and pitch responses of a semi-submersible are estimated by multiplying the JONSWAP spectrum by the RAOs obtained from ANSYS AQWA. Moreover, the long-term obtained by adopting both the 1D and 2D models are compared with those estimated by the full long-term approach.

The 1D model results in a nearly linear significant wave height behaviour and accordingly peak period behaviour. This behaviour is no longer linear with the 2D model. 60 tangent lines are used to construct the 2D environmental contours, which results in a visually smooth contour.

The 1D model compares well with the 2D model in the linear behaviour. Adopting the 1D model results in increasing Hs by 3.7% and Tp by 1.2%, whereas adopting the 2D results in increasing Hs by 3.13% and Tp by 1.46% in the linear domain.

The 2D model produces more realistic results than the 1D model. The later results in a maximum heave, surge and pitch response at only one sea state. However, the 2D model provides the sea states that causes the maximum of each response individually.

The results of the environmental contour method and the full long-term analysis are also compared. A remarkable deviation is observed, which agree well with Saranyasoontorn & Manuel (2004), except for the heave long-term response. This is expected due to the peak periods resulting from the 2D model, that are approaching the natural period of heave motion, which is equal to 17.1 s.

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